

Name \_\_\_\_\_

Date \_\_\_\_\_ Block \_\_\_\_\_

# Factoring Practice (Review)

## I. Greatest Common Factor (GCF)

Find the GCF of the numbers.

$$\begin{array}{l} 18, 30 \\ 18 = 2 \cdot 3 \cdot 3 \\ 30 = 2 \cdot 3 \cdot 5 \\ 2 \cdot 3 = 6 \\ 6 = \text{GCF} \end{array}$$

1. 12, 18
2. 10, 35
3. 8, 30
4. 16, 24

5. 28, 49
6. 27, 63
7. 30, 45
8. 48, 72

## II. Greatest Common Monomial Factor

Factor, write prime if prime.

$$12a^3b + 15ab^3 = 3ab(4a^2 + 5b^2)$$

1.  $6x + 3$
2.  $24x^2 - 8x$
3.  $6x - 12$
4.  $2x^2 + 8x$
5.  $4x + 10$
6.  $10x^2 + 35x$
7.  $10x^2y - 15xy^2$

8.  $12x^2 - 9x + 15$
9.  $3n^3 - 12n^2 - 30n$
10.  $9m^2 - 4n + 12$
11.  $2x^3 - 3x^2 + 5x$
12.  $13m + 26m^2 - 39m^3$
13.  $17x^2 + 34x + 51$
14.  $18m^2n^4 - 12m^2n^3 + 24m^2n^2$

## III. Factoring the Difference of Two Squares

$$\begin{array}{l} a^2 - 36 = (a + 6)(a - 6) \\ 3x^2 - 48 = 3(x^2 - 16) = 3(x + 4)(x - 4) \end{array}$$

Factor, write prime if prime.

1.  $x^2 - 1$
2.  $x^2 - 9$
3.  $x^2 + 4$
4.  $x^2 - 25$
5.  $9y^2 - 16$
6.  $4x^2 - 25$
7.  $9x^2 - 1$
8.  $a^2 - x^2$
9.  $25 - m^2$
10.  $x^2 - 16y^2$
11.  $25m^2 - n^2$

12.  $-x^2 + 16$
13.  $36m^2 - 121$
14.  $2x^2 - 8$
15.  $25 + 4x^2$
16.  $4a^2 - 81b^2$
17.  $12x^2 - 75$
18.  $a^2b - b^3$
19.  $-98 + 2x^2$
20.  $5x^2 - 45y^2$
21.  $9x^4 - 4$
22.  $16x^4 - y^2$

#### IV. Factoring Perfect Square Trinomials

$$x^2 - 14x + 49 = (x - 7)^2$$

Factor, write prime if prime.

1.  $x^2 + 8x + 16$

2.  $x^2 - 16x + 64$

3.  $y^2 + 12y + 36$

4.  $a^2 - 10a + 25$

5.  $16y^2 + 8y + 1$

11.  $25a^2 + 60a + 36$

12.  $16 + 40x + 25x^2$

13.  $16x^2 + 24x + 9$

14.  $49x^2 - 14x + 1$

15.  $9y^2 - 30y + 25$

6.  $9x^2 - 6x + 1$

7.  $25x^2 + 10x + 1$

8.  $n^2 - 14n + 49$

9.  $81x^2 - 90x + 25$

10.  $4y^2 - 20y + 25$

16.  $n^2 + 2n + 1$

17.  $b^2 + 2b + 1$

18.  $36x^2 + 84x + 49$

19.  $81 - 18x + x^2$

20.  $4 - 12y + 9y^2$

#### V. Special Factoring - Challenge

Factor, write prime if prime.

1.  $a^2 - 36$

2.  $9x^2 - 49$

3.  $169m^2 - 4u^2$

4.  $x^2y^2 - 9z^4$

5.  $\frac{1}{4}x^2 - 25y^2$

6.  $\frac{1}{9}x^2 - 16$

7.  $64 - a^4b^4$

8.  $y^6 - 100$

9.  $\frac{4}{9}x^2y^2 - \frac{25}{36}z^2$

10.  $y^8 - 81$

11.  $1 - 8u + 16u^2$

12.  $a^2b^2 + 6ab + 9$

13.  $x^2 + 2xy + y^2$

14.  $4x^2 + 12xy + 9y^2$

15.  $100h^2 + 20h + 1$

16.  $9a^2 - 24a + 16$

17.  $4a^3 + 8a^2 + 4a$

18.  $5c + 20c^2 + 20c^3$

19.  $(x + 4)^2 - (y + 1)^2$

20.  $(x - 1)^2 - 10(x - 1) + 25$

#### VI. Factoring Trinomials: $x^2 + bx + c$

$$x^2 + 7x + 10 = (x)^2 + (2 + 5)x + (2)(5) = (x + 2)(x + 5)$$

$$\begin{array}{r|l} x^2 + 7x + 10 & \\ \hline 10 & 7 \\ 5, 2 & \end{array}$$

Factor, write prime if prime.

1.  $x^2 + 6x + 8$

2.  $c^2 + 5c + 6$

3.  $y^2 - 9y + 14$

4.  $x^2 - 10x + 16$

5.  $a^2 + 12a + 27$

6.  $x^2 - 14x + 24$

7.  $x^2 - 15x + 36$

8.  $y^2 + 21y + 54$

9.  $m^2 + 13m - 36$

10.  $x^2 - 8x + 15$

11.  $y^2 - 4y - 32$

12.  $x^2 - x - 6$

13.  $y^2 + 3y - 18$

14.  $b^2 + 7b - 18$

15.  $a^2 + a - 56$

16.  $c^2 - 4c - 12$

17.  $x^2 - 9x - 36$

18.  $y^2 + 4y - 21$

19.  $x^2 - 22x - 75$

20.  $x^2 - 3x - 40$

21.  $45 + 14y + y^2$

22.  $x^2 - 13x + 36$

# VII. ...More Factoring Trinomials: $x^2 + bx + c$

$$k^2 - k - 20 = (k)^2 + (4 + -5)k + (4)(-5) = (k + 4)(k - 5)$$

Factor, write prime if prime.

1.  $x^2 + 7x + 12$
2.  $m^2 + 10m + 21$
3.  $y^2 - 7y - 8$
4.  $x^2 - 6x + 5$
5.  $x^2 + 4x - 32$
6.  $x^2 - 2x - 15$
7.  $x^2 - 6x + 8$
8.  $y^2 + 9y + 18$
9.  $3 - 4t + t^2$
10.  $v^2 + 12v + 20$

11.  $51 - 20k + k^2$
12.  $a^2 - 14ab + 24b^2$
13.  $y^2 + 6y - 72$
14.  $x^2 - 11xy - 60y^2$
15.  $15r^2 + 2rs - s^2$
16.  $3x^2 + 21xy - 54y^2$  (Hint: Check for GCF)
17.  $x^2 - 5xy - 6y^2$
18.  $x^2 + 8xy + 12y^2$
19.  $y^2 - 7xy + 10x^2$
20.  $a^2 - 11ab - 60b^2$

# VIII. Factoring Trinomials: $ax^2 + bx + c$

$$2x^2 - 5x - 3 = (2x + 1)(x - 3)$$

$\begin{matrix} *a \cdot c \\ -6 \end{matrix}$	$\begin{matrix} +b \\ -5 \end{matrix}$
$-6, 1$	

$$\begin{aligned} &2x^2 - 5x - 3 \\ &\quad \wedge \\ &2x^2 - 6x + 1x - 3 \\ &2x(x - 3) + 1(x - 3) \\ &(2x + 1)(x - 3) \end{aligned}$$

Factor, write prime if prime.

1.  $2x^2 - 5x - 3$
2.  $3x^2 + 10x - 8$
3.  $2y^2 + 15y + 7$
4.  $7a^2 - 11a + 4$
5.  $5n^2 + 17n + 6$
6.  $4y^2 + 8y + 3$
7.  $3x^2 + 4x - 7$
8.  $2x^2 + 13x + 15$
9.  $9y^2 + 6y - 8$
10.  $6x^2 - 7x - 20$

11.  $2n^2 - 3n - 14$
12.  $5n^2 + 2n + 7$
13.  $10x^2 + 13x - 30$
14.  $12y^2 + 7y + 1$
15.  $2n^2 + 9n - 5$
16.  $2x^2 + 7x + 6$
17.  $5a^2 - 42a - 27$
18.  $15x^2 - 28x - 32$
19.  $8a^2 - 10a + 3$
20.  $2y^2 - 3y - 20$

# IX. ...More Factoring Trinomials: $ax^2 + bx + c$

Factor, write prime if prime.

1.  $3x^2 + 4x + x$
2.  $5z^2 + 7z + 2$
3.  $2n^2 - 11n + 5$
4.  $3z^2 + z - 2$
5.  $5h^2 - 2h - 7$
6.  $8s^2 - 10st + 3t^2$
7.  $6x^2 + 19x + 15$
8.  $28a^2 + 5ab - 12b^2$

9.  $2a^2 + 7ab - 15b^2$
10.  $12x^2 + 17x + 6$
11.  $4a^2 - 4ab - 5b^2$
12.  $56y^2 + 15y - 56$
13.  $12x^2 - 29xy + 14y^2$
14.  $64x^2 + 32xy - 21y^2$
15.  $16x^2 + 56xy + 49y^2$
16.  $18x^2 - 57x + 35$

## X. Factoring: Putting It All Together

$$5x^2 + 20x - 60 = 5(x^2 + 4x - 12) = 5(x + 6)(x - 2)$$

Factor Completely, write prime if prime.

- |                      |                          |
|----------------------|--------------------------|
| 1. $2x^2 - 8$        | 9. $4x^2 + 16x + 16$     |
| 2. $2x^2 + 8x + 6$   | 10. $18x + 12x^2 + 2x^3$ |
| 3. $3n^2 + 9n - 30$  | 11. $2x - 2xy^2$         |
| 4. $6x^2 - 26x - 20$ | 12. $3t^3 - 27t$         |
| 5. $2x^2 + 12x - 80$ | 13. $24a^2 - 30a + 9$    |
| 6. $5t^2 + 15t + 10$ | 14. $10x^2 + 15x - 10$   |
| 7. $8n^2 - 18$       | 15. $3x^2 - 42x + 147$   |
| 8. $14x^2 + 7x - 21$ | 16. $4x^4 - 4x^2$        |

## XI. ...More Factoring: Putting It All Together

- |                         |   |
|-------------------------|---|
| 1. $16x^2 - 40x - 24$   | 8. $x^4 - 3x^2 - 4$                           |
| 2. $27x^2 - 36x + 12$   | 9. $h^2 - (a^2 - 6a + 9)$                     |
| 3. $5x^2 - 60x - 140$   | 10. $81x^4 - 16y^4$                           |
| 4. $6m^3 + 54m^2 - 6m$  | 11. $4mn^2 - 4m^2n^2 + m^3n^2$                |
| 5. $5k^4 + 8k^3 - 4k^2$ | 12. $(2a + 3)^2 - (a - 1)^2$                  |
| 6. $x^2y^4 - x^6$       | 13. $16d^8 - 8d^4 + 1$                        |
| 7. $y^4 - 6y^2 - 16$    | 14. $x^2(x^2 - 4) + 4x(x^2 - 4) + 4(x^2 - 4)$ |

## XII. Extra: Factoring by Grouping

$$\begin{aligned} 6ax - 2b - 3a + 4bx &= 6ax - 3a + 4bx - 2b \\ &= 3a(2x - 1) + 2b(2x - 1) \\ &= (2x - 1)(3a + 2b) \end{aligned}$$

- |   |                                  |
|---|----------------------------------|
| 1. $x^2 + 2x + xy + 2y$                         | 8. $n^2 + 2n + 3mn + 6m$         |
| 2. $3a^2 - 2b - 6a + ab$                        | 9. $2ax^2 + bx^2 - 2ay^2 - by^2$ |
| 3. $t^3 - t^2 + t - 1$ Hint: $t - 1 = 1(t - 1)$ | 10. $yz^2 - y^3 + z^3 - y^2z$    |
| 4. $10 + 2t - 5s - st$                          | 11. $y^3 - y^2 - 4y + 4$         |
| 5. $\frac{2}{3}bc - \frac{14}{3}b + c - 7$      | 12. $x^2a + x^2b - 16a - 16b$    |
| 6. $4u^2 + v + 2uv + 2u$                        | 13. $x^3 + x^2 - x - 1$          |
| 7. $ad + 3a - d^2 - 3d$                         | 14. $a^3 - a^2 - 8a + 8$         |